

**FLUID STRUCTURE SIMULATION OF A LEFT VENTRICLE
WITH DILATED CARDIOMYOPATHY**

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ABSTRACT

Dilated cardiomyopathy (DCM) is the most common myocardial disease which not only leads to systolic dysfunction but also diastolic deficiency. In the present work, the effect of DCM on the intraventricular fluid dynamics and myocardial wall mechanics were investigated. In addition, the individual effect of parameters related to DCM on several important fluid dynamics and myocardial wall mechanics variables during ventricular filling were also studied. Intraventricular fluid dynamics and myocardial wall deformation are significantly impaired under DCM conditions, which were demonstrated by low vortex intensity, flow propagation velocity (V_p), intraventricular pressure difference (IVPD), and strain rates, but high end diastolic pressure (EDP) and wall stress. The sensitivity analysis results showed that V_p substantially decreases with an increase in wall stiffness, and is relatively independent of preload at low peak E-wave velocity. Early IVPD is mainly affected by the rate of change of the early filling velocity and end systolic volume (ESV) which changes the ventriculo:annular proportion. Regional strain rate, on the other hand, is significantly correlated with regional stiffness, and therefore forms a useful indicator for myocardial regional ischemia. This study enhanced understanding of the mechanisms leading to clinically observable changes in patients with DCM.

ABSTRAK

“Dilated cardiomyopathy” (DCM) adalah merupakan penyakit miokardium yang paling umum di mana bukan sahaja membawa kepada ketidakcekapan sistolik tetapi juga diastolik. Dalam kajian ini, kesan DCM pada dinamik bendalir intraventrikel dan mekanik dinding miokardium telah diselidiki. Di samping itu, kesan parameter yang berkaitan dengan DCM kepada individu berkaitan dengan beberapa dinamik bendalir yang penting dan pembolehubah miokardium mekanik semasa pengisian ventrikel turut dikaji. Dinamik bendalir dalam ventrikel dan perubahbentukan miokardium terjejas dengan ketara di bawah keadaan DCM, yang telah ditunjukkan oleh keamatan vorteks yang rendah, halaju penyebaran aliran (V_p), perbezaan tekanan dan kadar terikan intraventrikel (IVPD), tetapi menunjukkan tekanan akhir diastolic (EDP) dan tegasan dinding yang tinggi. Keputusan sensitiviti analisis menunjukkan bahawa halaju penyebaran aliran berkurangan secara ketara dengan peningkatan kekukuhan dinding, dan agak tidak bergantung kepada prabeban pada halaju puncak “E-wave” yang rendah. IVPD awal terutamanya dipengaruhi oleh kadar perubahan halaju pengisian awal dan kelantangan sistolik akhir (ESV) yang mengubah perkadaran “ventriculo:annular”. Sebaliknya, kadar terikan kawasan mempunyai hubungan yang signifikan dengan kekukuhan kawasan, dan oleh itu membentuk petunjuk yang berguna untuk iskemia kawasan miokardium. Kajian ini meningkatkan pemahaman tentang mekanisme yang membawa kepada perubahan klinikal yang dapat dilihat pada pesakit DCM.

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LIST OF ABBREVIATIONS

ALE	Arbitrary Lagrangian-Eulerian
CFD	Computational Fluid Dynamics
DT	Deceleration Time
DCM	Dilated Cardiomyopathy
EDP	End Diastolic Pressure
EF	Ejection Fraction
EDV	End Diastolic Volume
ESV	End Systolic Volume
FSI	Fluid Structural Interaction
V_p	Flow Propagation Velocity
ICM	Ischemic Dilated Cardiomyopathy
IDCM	Idiopathic Dilated Cardiomyopathy
IVPD	Intraventricular Pressure Difference
IVPD_E	Early Intraventricular Pressure Difference
IVPD_L	Late Intraventricular Pressure Difference
LV	Left Ventricle

LVAD Left Ventricular Assist Device

PV Pressure-Volume

SI Sphericity Index

vMs Von Mises Stress

LIST OF SYMBOLS

Ω_s	Antisymmetric velocity gradient tensor
$\overline{\omega}$	Average vorticity
σ_θ	Circumferential wall stress
μ	First material constant of Ogden constitutive equation
ρ	Fluid density
\mathbf{u}_f	Fluid displacement vector
p	Fluid pressure
$\boldsymbol{\sigma}_f$	Fluid stress tensor
\mathbf{v}	Fluid velocity vector
η	Fluid viscosity
σ_ϕ	Meridional wall stress
S	Nominal stress
α	Second material constant of Ogden constitutive equation
\mathbf{u}_s	Solid displacement vector
$\boldsymbol{\sigma}_s$	Solid stress tensor
W	Strain energy function

λ	Stretch
Ω_s	Symmetric velocity gradient tensor
\mathbf{n}	Unit normal vector
Γ_1	Vortex intensity
ω	Vorticity

Chapter 1. INTRODUCTION

This chapter provides a preface of the present work. The introduction is initiated by research motivation and extends to the objectives of this research. An outline of thesis organisation and synopsis of each chapter are available in the last part of introduction.

1.0. Research motivation

Heart failure is characterized by the inability of the heart to supply adequate blood flow and therefore oxygen delivery to tissues and organs in the body. Cardiovascular disease is the most commonly reported cause of mortality and it contributes to approximately 30 percent of deaths. In order to maintain cardiac output, compensatory mechanisms take place, including geometrical modifications of the heart (remodelling). The heart is stretched to hold more blood in the diastole so that it is able to generate stronger force of contraction during systole, following the Frank Starling's law (Patterson et al., 1914; Sarnoff & Berglund, 1954; Starling & Visscher, 1926). Furthermore, to overcome high afterload pressure normally experienced by these patients, yet with reasonable wall stress, the muscle wall thickens. Over a long period, the gradual declination of cardiac performance is no longer compensable which then develops into heart failure. Dilated cardiomyopathy (DCM) is the most common cardiomyopathy disease which has been frequently reported incidence of morbidity and mortality, with a mortality rate of up to 50% annually in patients with idiopathic DCM (IDCM) (Zipes & Wellens, 1998).

Numerous methods have been used to diagnose and differentiate various types of heart failure conditions in order to plan for the best treatment strategies for the

patients. These involve examining the heart's morphology (Altbach et al., 2007; Amano et al., 2004; Somauroo et al., 2001), electrical activity (Narayana, 2011; Rosen et al., 1979), mechanics (Altbach et al., 2007; Augenstein et al., 2001; Kirkpatrick & Lang, 2008) and hemodynamics (Feintuch et al., 2007; Thomas, J. D. & Popovic, 2006). With the advancement of medical technologies, non-invasive imaging modalities, such as chest x-ray, electrocardiogram, computed tomography, magnetic resonance imaging (MRI) are gradually becoming more popular. Among these, MRI and echocardiography are the most commonly used diagnostic tools to assess cardiac function through geometric and flow measurements, such as left ventricle (LV) volume, wall mass, stroke volume, ejection fraction (EF), wall motion and wall thickness. The global LV function depends on both systolic and diastolic function. As in DCM case, clinical imaging modalities report systolic dysfunction by EF reduction (Dahm et al., 2002; Persson et al., 1995) however the gauge of diastolic dysfunction is not yet well-founded.

Alternatively, Computational Fluid Dynamics (CFD) method which involves the study of cardiovascular blood flow pattern has emerged as a reliable tool in enhancing the understanding of the pathophysiology and progression of the heart disease, by easily allowing reproducible numerical experiments under identical conditions. Both of the global and regional hemodynamic variables are feasible through the simulations. Regional hemodynamic variables are, for instance, pressure distributions, myocardial strains, and stresses. The velocity fields and shear stress have a complicated relationship in thrombus formation (Taylor & Draney, 2004) which is important in identification of cardiac disease. Hereby various physical flow conditions can be predicted while induce early recognition of disease stage helps to reduce patient's risk. As a result, CFD

simulation has been extensively applied in the investigation of ventricle pathological flow (del Alamo, 2009; Ge & Ratcliffe, 2009) and evaluation of surgical treatment and cardiac assist device. Thereby strong comprehension in pathophysiology of DCM is to be developed through CFD study in the present work.

1.1. Research objectives

The aim of this work is to investigate the effect DCM LV on intraventricular fluid dynamics and myocardial wall mechanics. The overall objective of this work is to perform a simulation of DCM LV during diastolic filling phase. In addition, the individual effects of parameters related to DCM are also to be evaluated through sensitivity analysis. They are the peak E-wave velocity, end systolic volume (ESV), wall stiffness and sphericity index (SI) on intraventricular fluid dynamics and myocardial wall mechanics during LV filling. In order to achieve the aim of the study, the following objectives were established:

1. To develop a simplified model of the LV with DCM,
2. To simulate the diastolic filling of LV with DCM,
3. To investigate fluid and mechanical variables in the LV with DCM during the diastolic filling phase and compare the results to the published studies,
4. To conduct sensitivity analysis and evaluate the effect of individual parameter which contribute towards DCM.

1.2. Research Question

The study attempts to answer the following research questions:

1. What velocity profile characterizes the blood travelling through mitral valve during filling phase?
2. Which CFD method is more suitable to be used for the investigation of intraventricular hemodynamic and wall mechanics of a LV with DCM?
3. What are the impacts on intraventricular hemodynamic and wall mechanics in LV with DCM compared to a normal LV?
4. What are the effects of individual parameters which contribute towards DCM?

1.3. Thesis organization

The thesis is composed of six chapters. Chapter 2 provides the literature review done on DCM in both clinical and simulation situations. Chapter 3 explains the implementation of this work in full details; from the selection of boundary condition (i.e. transmitral velocity profile) and CFD method either geometry-prescribed or fluid-structure interaction (FSI), to the complete DCM simulation which incorporates both blood flow and myocardial properties. Chapter 4 describes the simulation outcome where the different sets of results were compared and analyzed. Chapter 5 compares the results in Chapter 4 to previous studies and discuss them. Chapter 6 concludes the findings of the present work and provides suggestions for future improvements.

Chapter 2. LITERATURE REVIEW

2.0. Introduction

DCM is one of the most common cardiac diseases characterized by myocardial contractile dysfunction and ventricular dilatation with a change of sphericity (from an elliptical to a spherical shape) (Douglas et al., 1989; Jefferies & Towbin, 2010). In addition, patients with DCM have a stiffer myocardial wall, caused by increased myocardial mass and alteration in the extracellular collagen network (Gunja-Smith et al., 1996). The measureable functional deficiencies of DCM include low EF and decreased wall motion (Plein et al., 2001).

DCM can be caused by many factors, such as genetic, infection, alcohol abuse as well as other cardiac diseases. Generally, the etiology of DCM is classified into ischemic and non-ischemic. The IDCM, primary myocardial damage, is the most common among the non-ischemic group. It arises spontaneously and has unknown causes. Ischemic DCM (ICM) experiences secondary myocardial damage as a result of poor perfusion of the myocardial wall caused by the coronary disease. Irrespective of the disease etiology, all DCM patients experience similar mechanical compensation. Despite having a similar mechanical compensation and global hemodynamics, Parodi et al. (1993) observed a more heterogeneous transmural blood flow distribution in patients with ICM and a higher percentage of fibrosis in these patients in their clinical studies as compared to patients with IDCM (Parodi et al., 1993). Not limited to clinical studies, this chapter also traced the findings of DCM through computational models which are described in the sections below.

2.1. Clinical imaging studies

The structural ventricular remodelling processes associated with DCM, including chamber enlargement, alterations in shape and decreased wall compliance significantly affect the intraventricular filling dynamics. Commonly under measurement of MRI (Imai et al., 1992) and echocardiography (Donal et al., 2009; Rihal et al., 1994; Thomas, D. E. et al., 2009), it shows increased EDV (greater than 112 percent) and ESV with thinner wall in anatomical data while functionally with low EF (less than 45 percent) and decrease wall motion with fractional shortening less than 25 percent. Mitral regurgitation flow was found as hemodynamic disorders (Donal et al., 2009).

Experimental study (Ohno et al., 1994) has reported that transmitral filling pattern revealed progression of heart disease due to gradual decrease of wall compliance and increase of LV pressure. The impaired relaxation filling pattern indicates an early stage of diastolic dysfunction (Grade I), followed by a more severe pseudonormal filling pattern (Grade II). The restrictive filling pattern (Grade III-IV) implies the most advanced disease stage (Nishimura & Tajik, 1997).

Extensive clinical studies have investigated the difference between normal subjects and DCM patients with regards to the intraventricular fluid dynamics (e.g. flow propagation velocity, V_p (Garcia et al., 1998), intraventricular pressure difference (IVPD) (Yotti et al., 2005), vortex area and intensity (Hong et al., 2008)) as well as myocardial wall mechanics (e.g. principal strain (Tibayan et al., 2003) and strain rate (Støylen et al., 2001; Wang et al., 2007)) using different imaging modalities, including phase contrast magnetic resonance imaging (MRI) (MacGowan et al., 1997; Veress et

al., 2005), colour M mode echocardiography (Garcia et al., 1998), contrast echocardiography (Hong et al., 2008), and tissue Doppler imaging (Park et al., 2006; Støylen et al., 2001).

One limitation of these studies is that controversial findings often exist as there is a high variability among patient characteristics, and it is difficult to ascertain the effect of individual physiological variables on the parameters of interest (Garcia et al., 1998). For example, an increase in V_p was found in patients with moderate hypertrophy (Støylen et al., 2001), as opposed to other studies which demonstrated reduced V_p in patients with reduced diastolic function (Rodriguez et al., 1996). Furthermore, limitations in the measurement methods also contribute to the inconsistent findings. For an instance, strain measurements using Doppler-derived analysis face the problem of angle dependency (Gjesdal et al., 2008) while IVPD measurements using colour Doppler M-mode images may yield high error when applied on severely dilated ventricles (Yotti et al., 2005).

To overcome this problem, CFD and computational structural mechanics, which quantify the spatial and temporal distributions of the velocity, pressure, stress and strain in the heart, have emerged as reliable tools in enhancing the understanding of the pathophysiology and progression of structural heart disease.

2.2. CFD simulation studies

CFD approach provides approximate solution of velocity and pressure fields through Navier-Stokes equation (Discacciati & Quarteroni, 2009). For its strength over current imaging diagnostic tools, CFD is able to further provide insights into significance of hemodynamic factors such as intraventricular flow dynamics, wall shear stress, mass transport and stagnation region (Nanduri et al., 2009). Early CFD techniques for hemodynamic simulations were mostly carried out on simplified geometries (Domenichini et al., 2009; Vierendeels et al., 2000). With the development of cardiac imaging techniques, patient-specific morphology and flow has been progressively used (Long et al., 2008; Saber et al., 2001; Schenkel et al., 2008), which provides valuable clinical information. Recently, FSI models which take into account the interaction between the blood and the cardiac wall have been developed (Cheng et al., 2005; Krittian et al., 2010; Lemmon & Yoganathan, 2000; Nordsletten et al., 2011; Watanabe et al., 2004b).

Prescribed geometry (Baccani et al., 2002b; Doenst et al., 2009; Domenichini & Pedrizzetti, 2011; Loerakker et al., 2008) and FSI method (Watanabe et al., 2004a) in CFD approach were used to study hemodynamic within LV chamber where the outcomes are both representatively. The geometry-prescribed method uses prescribed moving boundaries to simulate movement of the cardiac wall. On the other hand, the FSI approach takes into account the interaction between the fluid and the structure and provides additional important parameters such as myocardial deformation and wall stress.

2.2.1. Geometry-prescribed approach

One of the few DCM studies include the geometry-prescribed model by Baccani et al. (2002b), who analyzed the vortex dynamics in an axisymmetrical LV with DCM during filling. The pulsatile flow rate obtained from clinical data is applied as inlet boundary condition. The wall motion is prescribed with change of diameter and height of LV according to the pulsatile flow rate. It was observed that geometrical alteration of the LV in DCM decreases V_p which may lead to the formation of apical thrombus.

In another study, Loerakker et al. (2008) developed an axisymmetrical fluid dynamics model of the LV, coupled to a lumped parameter model of the complete circulation, to investigate the influence of a ventricular assist device on the vortex dynamics in a ventricle with DCM. The lumped parameter model consists of systemic and pulmonary circulation make up by ventricular chamber, valves, venous and arteries in electrical circuit. A left ventricular assist device (LVAD) was modelled by connecting a flow pump between LV and aorta. The volume change in LV was derived from circulatory model and used to obtain fluid or wall velocity. With increasing flow rate in LVAD, it was found that ventricular volume decreased and EF raised up which shift the pressure-volume (PV) loop to the left. With assistance of LVAD in DCM heart, the flow field was corrected to be similar as in normal heart. The increase of LVAD flow rate decreased the LV volume and vortex formation is more effective. The vortex strength, area and vorticity are also improved.

The major limitation of the previous work is the interaction between blood flow and myocardial wall deformation, which significantly affects the various parameters of interest, has not been taken into account.

2.2.2. FSI approach

It is known that CFD greatly contributes to cardiac diagnosis with condition that accuracy of simulation result is promised. Due to limitation in certain aspect, assumptions always are made in CFD method. As such, result validation is important where well-matched outcome with imaging modalities and experiment helps in justification. In order to have acceptably accurate result, the CFD settings should be as realistic as possible. Cardiovascular CFD studies have progressively step forward to FSI method which tends to provide more realistic cardiac flow analysis.

In most of ventricular studies, the condition of normal LV is assessed by using FSI approach (Cheng et al., 2005; Krittian et al., 2010; Watanabe et al., 2002). Both of fluid and wall mechanics match closely with the reported outcome from clinical studies. Although numerous models of ventricular biomechanics for the ventricles have been published (Khalafvand et al., 2011), they have not been widely used in the study of diseased states. One of the few diseased ventricle models includes myocardial infarction ventricle modelled by Watanabe et al. (2004a). To the best of author's knowledge, there is no DCM model that has been presented using FSI approach.

2.3. Conclusion

Due to the limitations of current cardiac imaging modalities, CFD has been widely used in cardiac function assessment and heart disease diagnosis as it can provide further insight into cardiac flow field. The understanding of ventricular hemodynamics and pathological severities were explored through CFD method. However, assumptions are always made in CFD method. As such, the result validation is important where well-matched outcome with imaging modalities and experiment help in justification. In order to have exact compatible results, the CFD boundary conditions should be as realistic as possible. However, the existing DCM studies were confined on standalone study of blood flow dynamics and wall mechanics instead of more realistic two ways interaction between blood and myocardium. Thus, this research study will develop more insight in DCM investigation by using FSI approach in CFD implementation.

Chapter 3. METHODOLOGY

3.0. Introduction

Before the simulation of DCM state, the selection of boundary conditions (uniform versus parabolic transmitral velocity profile) and CFD method (geometry-prescribed versus FSI approach) were compared in order to confirm the precise simulation conditions. As such, the methodology was divided into four parts. The first two sections involved investigation of transmitral spatial velocity profile and CFD simulation approach, respectively. Subsequently, the complete simulation of DCM conditions, including the detailed blood flow settings and myocardial properties, were described. The last part of methodology explained the sensitivity analysis used to evaluate individual factors which weaken the DCM LV. All the simulations were performed by the commercial simulation software, COMSOL Multiphysics Inc.

3.1. Investigation on transmitral spatial velocity profile

The laminar flow model is applied due to the relatively low intraventricular blood flow velocity (Cheng et al., 2005), which cause to a low Reynolds number (≈ 150). In order to verify the spatial velocity profile, two different laminar transmitral velocity profiles were imposed across the mitral orifice, i.e. uniform velocity profile and parabolic velocity profile. Figure 3.1 shows the spatial velocity profile at the mitral orifice during peak of E wave. In the figure, only half of the valve diameter is shown due to the axisymmetric representation, where left side of x-axis represents middle of the valve while right side of x-axis represents edge of the valve. The velocity is constant

throughout the mitral valve using the uniform velocity profile setting while the parabolic velocity profile setting shows the highest velocity occurring at the middle of the mitral valve where the peak velocity magnitude is about two-fold of uniform velocity profile. The transmitral flow velocity was directed to the mitral inlet of a dilated LV with ESV of 150 mL. For the purpose of this investigation, the geometry-prescribed approach was used as the LV wall properties were not decided yet at this stage of study.

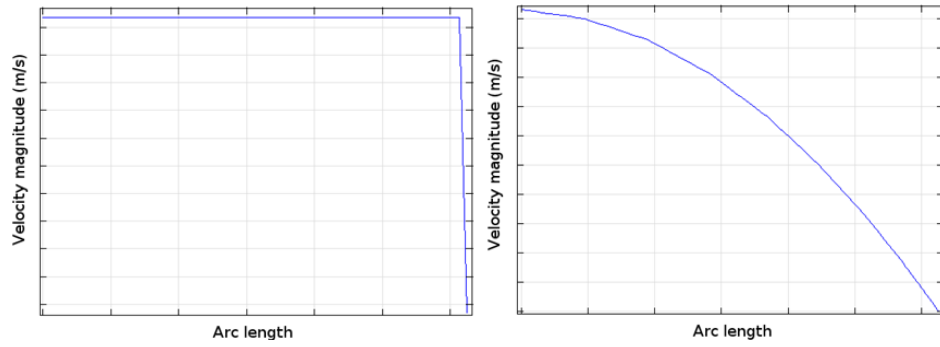


Figure 3.1: Spatial profile of inlet velocity at the mitral valve during peak of E wave, using different settings: uniform flow (left) and parabolic flow (right).

3.2. Investigation on CFD simulation approach

Theoretically, the quantitative blood flow dynamics was solved using the continuity (Equation 3.1) and incompressible Navier-Stokes equation (Equation 3.2):

$$\nabla \cdot \mathbf{v} = 0 \quad (3.1)$$

$$\rho \left(\frac{\partial \mathbf{v}}{\partial t} + \mathbf{v} \cdot \nabla \mathbf{v} \right) = -\nabla p + \eta \nabla^2 \mathbf{v} \quad (3.2)$$

where \mathbf{v} (m/s) is the fluid velocity vector and p (Pa) is the pressure. Blood is assumed to be Newtonian with constant density, ρ (1050 kg/m³) and viscosity, η (0.0035 Pa.s).

In this investigation section, three LV models with ESV of 50 mL, 150 mL and 300 mL were simulated and each LV represented size of normal, moderately dilated, and severely dilated correspondingly. A constant transmitral temporal velocity and uniform spatial velocity profile was imposed.

3.2.1. Geometry-prescribed method

The geometry-prescribed method proposed by Baccani et al. (2002b) was adapted, where the wall motion was derived from the instantaneous blood flow rate, $Q(t)$ (m^3/s) through the mitral valve on the basis of a simple elastic membrane model. The rate of change of the ventricular base equatorial radius, R (m), and the ventricular height, H (m) are as shown in the Equation 3.3 and 3.4, respectively:

$$\frac{dR}{dt} = \frac{3Q(t)}{\pi} \frac{2H^2 - R^2}{10H^3R - 4HR^3} \quad (3.3)$$

$$\frac{dH}{dt} = \frac{3Q(t)}{\pi} \frac{H^3}{2H^2R - R^3} \frac{2H^2 - R^2}{10H^3R - 4HR^3} \quad (3.4)$$

The derivation of Equation (3.3) and (3.4) are shown in the Appendix.

3.2.2. FSI method

By using the FSI method, the LV wall deformed accordingly when blood filled the ventricular chamber, depending on the wall properties and the load imposed by the blood. The coupling between the blood and the myocardial wall was taken into account at the fluid-solid interface through the following relationship:

$$\mathbf{u}_f = \mathbf{u}_s \quad (3.5)$$

$$\boldsymbol{\sigma}_f \cdot \mathbf{n} = \boldsymbol{\sigma}_s \cdot \mathbf{n} \quad (3.6)$$

where \mathbf{u}_f , \mathbf{u}_s (m) represents the displacements, $\boldsymbol{\sigma}_f$, $\boldsymbol{\sigma}_s$ (Pa) represents the stress tensors of the blood and myocardial wall, respectively, at the fluid solid interface, and \mathbf{n} represents the unit normal vector.

In numerical scheme, an arbitrary Lagrangian-Eulerian (ALE) method was used to syndicate the blood flow formulated using an Eulerian description and a spatial frame, with myocardial wall mechanics formulated using a Lagrangian description and a material frame. To achieve model convergence, the myocardial wall mechanics formulation allowed large wall deformations, or also known as geometric nonlinearity. The blood flow spatial frame deformed with a mesh deformation that was equal to the myocardial wall displacements, \mathbf{u}_s . The wall motion was adjusted according to the free moving mesh inside the blood domain. This geometric change of the blood domain was automatically accounted for in COMSOL Multiphysics by the ALE method.

3.3. Simulation of DCM conditions

The complete DCM conditions were simulated using FSI approach, where the LV wall deformation was dependent on the wall properties and the load imposed by the fluid. However, it was noted that LV basal wall was fixed in all directions while other parts of the wall were allowed to move freely in the model settings. A 2D axisymmetrical model was used in the simulation. The assumptions made in this simulation study include:

1. The LV is a symmetrical half truncated prolate ellipsoid.
2. The mitral valve is a fixed opening orifice.
3. The LV wall is hyperelastic, incompressible and transverse isotropic.
4. Blood is incompressible and behaves as Newtonian fluid.

3.3.1. Disease conditions

In the present work, two DCM conditions were simulated in respective model: IDCM and ICM where the infarction was located at the apical wall region. The infarction region occupied 60 percent of the total wall region. The wall compliance of whole myocardial wall region was decreased homogeneously in IDCM. A normal LV was modelled in order to serve as baseline model for comparison with DCM conditions.

3.3.2. Geometry of LV

An axisymmetrical half truncated prolate ellipsoid was used to represent a normal LV while the half truncated prolate spheroid characterized DCM LVs. The SI was characterized by a ratio of ventricular radius at the equator plane to ventricular height from base to apex. The normal and DCM LVs appeared in SI of 0.52 and 0.62, respectively (Zhong et al., 2009). At the ventricular base, the mitral valve was modelled as a fixed opening orifice with 0.6 ventriculo:annular proportion for normal LV whereas 0.4 ventriculo:annular proportion for DCM LV. The ventriculo:annular proportion refers to the ratio of the LV radius to the radius of the mitral valve (or mitral annular ring). The aortic valve was closed throughout the filling phase. The LVs were modelled at the end systole initially and experience expanding volume during filling phase. The

normal LV was in ESV of 50 mL whereas 150 mL illustrated the DCM LVs. All LVs had wall thickness decreased along the ventricular wall from the base to the apex, with 11 mm at the base and 9 mm at the apex. The tetrahedral mesh was used in the simulation in COMSOL Multiphysics.

3.3.3. Material properties of LV wall

A hyperelastic wall with constant density of 1366 kg/m^3 (Watanabe et al., 2002) was used to represent the LV muscle in the passive state. As mentioned in Sub-section 3.3.2, the wall stiffness is constant throughout the whole ventricular wall for the normal and IDCM models. On the contrary, it is much higher at the apical region in the ICM model (60 percent of the total wall region) compared to other areas of the LV to simulate myocardial infarction. The parameter values were determined so that a predetermined EDP can be achieved for each condition.

The passive material model of Lin & Yin (1998) was adapted to represent ventricular biaxial stretch properties in this study. The Lin-Yin model was proposed based on the biaxially stretched rabbit specimens, by assuming the myocardium is hyperelastic, incompressible and transverse isotropic (Lin & Yin, 1998). It should be noted that the Lin & Yin (1988) model involved deduction of the functional form of strain energy function directly from the experimental data. The deduced strain energy function has been widely used because it was proven to give reproducible satisfactory stress-strain curve fits with the experimental data.

The material parameters (C_1 - C_4) of Lin & Yin (1998) passive model were determined so that an EDP of 9 mmHg is obtained in the normal LV. As a result, the material parameters were adjusted to 45 percent of reported average values. The material parameters were assumed as $C_1 = 46.34$ Pa, $C_2 = 4.11$, $C_3 = 1.044$, and $C_4 = 0.036$. Meanwhile, the DCM wall properties were characterized by adapting the passive material properties in diseased ventricles which have been employed by Watanabe et al. (2004a). The total strain energy density function as given in the Equation 3.7 is a combination of passive material model proposed by Lin & Yin (1998), (Equation 3.8) and Humphrey et al. (1990), (Equation 3.9):

$$W_{passive} = W_{LinYin} + mW_{Humphrey} \quad (3.7)$$

$$W_{LinYin} = c_1(e^Q - 1) \quad (3.8)$$

$$Q = c_2(I_1 - 3)^2 + c_3(I_1 - 3)(I_4 - 1) + c_4(I_4 - 1)^2$$

$$W_{Humphrey} = c_{1h}(I_4^{\frac{1}{2}} - 1)^2 + c_{2h}(I_4^{\frac{1}{2}} - 1)^3 + c_{3h}(I_1 - 3) + c_{4h}(I_1 - 3)(I_4^{\frac{1}{2}} - 1) + c_{5h}(I_1 - 3)^2 \quad (3.9)$$

In order to produce EDP of 20 mmHg in both DCM ventricles, the stress-strain relationship was adjusted through a scale factor, m in Equation 3.7. The scale factor, $m = 0, 3.5, 14$ and 100 were corresponded to ventricular wall properties of normal, ICM (base), IDCM, and ICM (apex), respectively. The material parameters of Humphrey et al. (1990) passive model were adopted ($C_{1h} = 1.97$ kPa, $C_{2h} = 6.212$ kPa, $C_{3h} = 0.164$ kPa, $C_{4h} = -2.7$ kPa, and $C_{5h} = 2.35$ kPa) (Humphrey et al., 1990). Figure 3.2 shows the LV wall stiffness (stress-strain curve) of normal LV, IDCM and ICM by comparing to Lin & Yin (1998) passive model and Watanabe et al. (2004a) infarction models.

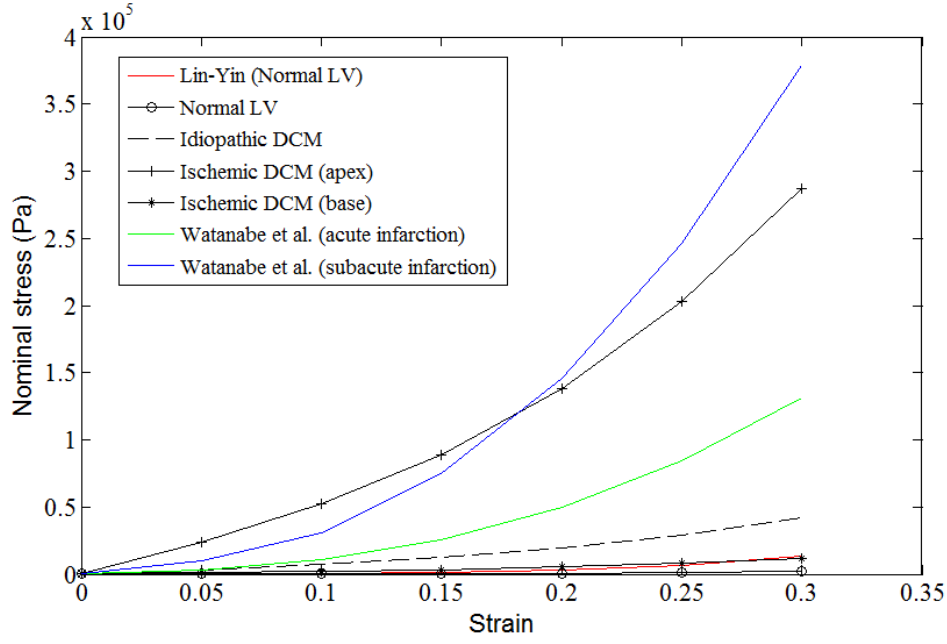


Figure 3.2: Stress-strain relationship.

Due to the fiber orientation in ventricular model not taken into consideration in the simulation, first-order Ogden constitutive relation in Equation 3.10 (Ogden et al., 2004) was selected to represent the biaxial stress-strain relationship of normal and DCM models for its advantages of simplicity as well as best curve fits with Lin-Yin passive model.

$$S = \frac{\mu}{\lambda} (\lambda^\alpha - \lambda^{-2\alpha}) \quad (3.10)$$

where S (kPa) represents nominal stress, λ represents principal stretch, while μ and α are material constants. The Ogden fitted curves were shown in Figure 3.3 where the semi-log plot (y-axis) on the right side was plotted in purpose for better visualization of different LV material properties.

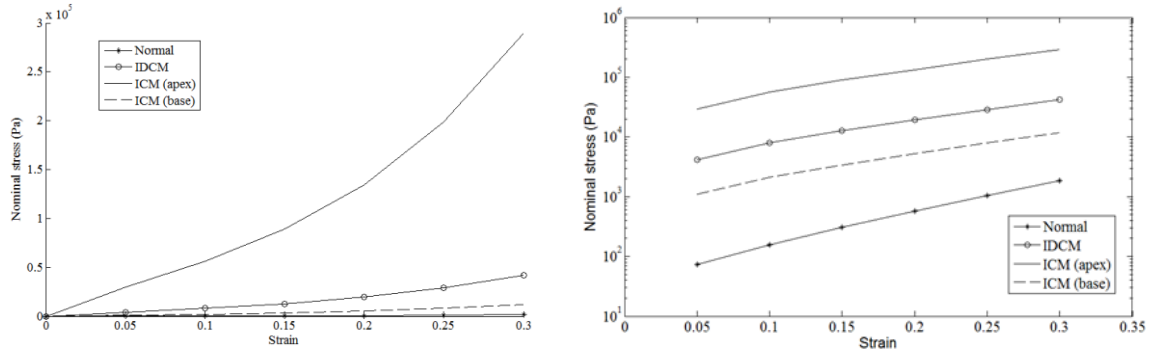


Figure 3.3: Relationship between nominal stress and strain for the normal, IDCM and ICM (basal and apical region) models. Semi-log plot (y-axis) is on the right.

3.3.4. Transmitral filling pattern

Blood was assumed to be incompressible and Newtonian, with a viscosity of 0.0035 Pa.s and a density of 1050 kg/m³ (Cheng et al., 2005). To simulate transmitral flow, a uniform velocity profile was applied at the inlet boundary representing the mitral valve. The time-varying profile of the filling phase comprised the E-wave, diastasis and A-wave, which represented the 3 main phases of the transmitral inflow.

Experimental study (Ohno et al., 1994) had reported that transmitral filling pattern revealed progression of heart disease due to gradual decrease of wall compliance and increase of LV pressure. The impaired relaxation filling pattern indicated an early stage of diastolic dysfunction (Grade I), followed by a more severe pseudonormal filling pattern (Grade II). The restrictive filling pattern (Grade III-IV) implied the most advanced disease stage (Nishimura & Tajik, 1997). Therefore, all four types of filling pattern were included in the present simulation study. A normal filling pattern with E/A

ratio of 1.6 and deceleration time (DT) of 200 ms were simulated for normal LV. Meanwhile, three filling patterns: impaired relaxation, pseudonormal, and restrictive filling were simulated for each DCM cases (IDCM and ICM).

Figure 3.4 shows transmitral velocity profile at normal condition and different stages of defect. For each of the filling pattern, E-wave refers to the first wave while A-wave refers to the second wave.

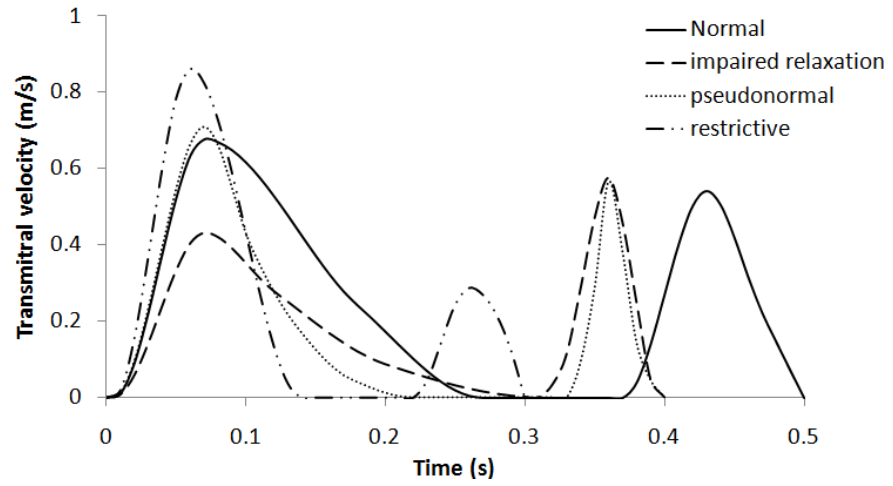


Figure 3.4: Temporal waveforms of the inlet velocity for normal, impaired relaxation, pseudonormal, and restrictive filling patterns.

In order to appropriately simulate the various conditions, ESV, filling velocity (including peak E-wave velocity, E/A ratio and E-wave DT), valve ratio, SI, and wall stiffness were varied accordingly to closely match the clinical measurements reported in the literature (Hayashida et al., 1990; Tulner et al., 2006; Yotti et al., 2005). Table 3.1 concluded the model settings of normal, IDCM, and ICM conditions.

Table 3.1: List of parameter values for normal, IDCM and ICM conditions.

	ESV (mL)	EDV (mL)	IV (mL)	VA	SI	EDP (mmHg)	E peak (m/s)	A peak (m/s)	DT (ms)	E/A	μ	α
Normal (baseline)	50	120	70	0.6	0.52	9.5	0.7	0.56	200	1.25	39.3	15.7
IDCM (IR)	150	194	44	0.4	0.62	20.3	0.45	0.6	250	0.75	3310	10.7
IDCM (PS)							0.74	0.59	160	1.25		
IDCM (RE)							0.9	0.3	70	3.0		
ICM (IR)	150	194	44	0.4	0.62	20.3	0.45	0.6	250	0.75	23705 (I)	10.5 (I)
ICM (PS)							0.74	0.59	160	1.25	843.2 (NI)	11.1 (NI)
ICM (RE)							0.9	0.3	70	3.0		

IR = impaired relaxation, PS = pseudonormal, RE = restrictive. ESV = end systolic volume, EDV = end diastolic volume, IV = total inflow volume, VA = ventriculo:annular proportion, SI = sphericity index, EDP = end diastolic pressure, E peak = peak E-wave velocity, A peak = peak A-wave velocity, DT = E-wave deceleration time, E/A = ratio of the peak E-wave velocity to the peak A-wave velocity, μ and α = material constants of the Ogden constitutive equation, NI = non-ischemic, I = ischemic.

3.4. Sensitivity analysis

The effects of a two-fold increase in the baseline normal value of peak E-wave velocity, ESV, wall stiffness, and SI on intraventricular fluid dynamics and myocardial wall mechanics were investigated. The outcomes to be compared include vortex parameters (average vorticity, vortex area, and vortex intensity), V_p , IVPD, as well as wall stress and strain rate.

3.4.1. Vortex identification

Average vorticity, $\bar{\omega}$ (1/s), was defined as the mean value of the out-of-plane vorticity ($\omega = |\nabla \times \mathbf{v}|$) in the LV. On the other hand, quantitative evaluation of the vortex area (Γ_A) and intensity Γ_I were carried out by first identifying the vortical regions in the LV using the λ_2 criterion proposed by Jeong et al. (1995). The eigenvalues ($\lambda_1, \lambda_2, \lambda_3$) of the tensor $\Omega_s^2 + \Omega_a^2$ are computed, where Ω_s and Ω_a are the symmetric and anti-symmetric parts of the velocity gradient tensor ($\nabla \mathbf{v}$) respectively. Assuming that $\lambda_1 > \lambda_2 > \lambda_3$, vortical regions were identified as regions with $\lambda_2 < 0$. Vortex intensity, Γ_I was thus calculated as in Equation 3.11:

$$\Gamma_I = \int_A \omega \, dA \quad (3.11)$$

where A (m^2) is the area of the vortical regions. The vortex area, Γ_A (m^2), is defined as the total area of the vortical regions. V_p (m/s) is calculated as the average travelling velocity of the peak E-wave velocity mid-way into the LV axis from the inlet.

3.5. Mesh dependency test

The mesh dependency was conducted in order to ensure selection of appropriate mesh to produce significant simulation results in addition to reduce simulation time consumption. The mesh used in the current study composed of 1331 elements. The number of elements was increased to 2143 and 5505 extreme fine mesh elements. It was found that the differences in maximum vorticity between 1331 to 2143 and 5505 mesh elements (during peak filling wave) were 2.9 percent and 4.3 percent, respectively. The reduction of mesh elements to 840 caused 5.6 percent maximum vorticity reduction

compared to 1331 mesh elements. Thus, tetrahedral mesh with 1331 elements was chosen for the study because the result variation with finer mesh elements was within 5 percent.

3.6. Numerical result validation

According to mass conservation law, the transfers of matter in a close system must maintain a constant mass over time. The difference between inflow blood volume and changes of LV volume during filling phase was inspected and the volume difference was within 2 percent. Hence, the simulation results were validated as conforming to the mass conservation law.

Chapter 4. RESULTS

4.0. Introduction

The result is presented into four parts. The first part described the results obtained from two different spatial velocity profiles, i.e. uniform vs. parabolic transmitral velocity profile. The second part compared the results obtained from two different CFD implementations, i.e. prescribed geometry vs. FSI method. Section 4.3 is the core of current work which showed the result of the complete simulation of DCM conditions. Finally, the findings of sensitivity analysis including effects of peak E-wave velocity, ESV, wall stiffness, as well as SI on fluid dynamics and wall mechanics were presented.

4.1. Uniform vs. parabolic velocity profile

In order to confirm the spatial velocity profile of transmitral blood flow, two types of laminar inlet velocity profiles were simulated during the filling phase: uniform and parabolic velocity profiles using geometry-prescribed approach. The results were analysed based on vortex evolution pattern and vortex strength.

Distinctive vortex evolution patterns were observed between the two cases: transmitral flow velocity with uniform (Figure 4.1) and parabolic transmitral velocity profiles (Figure 4.2). In the ventricle with a uniform inlet velocity profile, the incoming flow stream is rolled up immediately after travelling through a short distance away from the mitral valve ($t = 0.15$ s). The redirected blood stream forms a vortex ring, preserving the kinetic energy of the incoming flow through the fast spinning velocity. The

attachment of the vortex ring attached at the mitral edge restricts its propagation. Although the attached vortex ring is still able to move closer to the lateral wall in the meantime towards the apex, its low vortex strength does not help to break the wake attachment at the mitral edge. The uniform flow stream hanging at the basal region experiences a small convective acceleration that is unable to overcome the local deceleration effect.

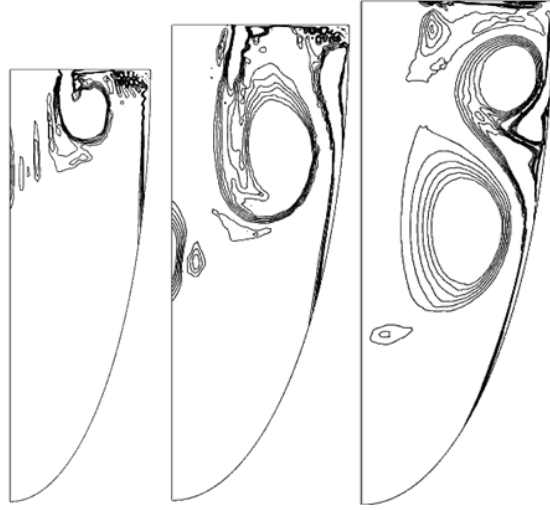


Figure 4.1: Vortex formation patterns obtained using uniform velocity profile as inlet boundary condition, instantaneous vorticity at $t = 0.15$ s (left), 0.25 s (middle) and 0.35 s (right), vorticity levels ($1/s$) from 5 to 100, step 10.



Figure 4.2: Vortex formation patterns obtained using parabolic velocity profile as inlet boundary condition, instantaneous vorticity at $t = 0.15$ s (left), 0.25 s (middle) and 0.35 s (right), vorticity levels ($1/s$) from 5 to 100, step 10.

During deceleration of the transmitral velocity ($t = 0.25$ s), kinetic energy decreases at the basal region while pressure decreases at the apical region. The change in the pressure and the velocity encourages the growth of the vortex ring and facilitates its detachment from the attached wake at a later time. The free vortex ring starts to propagate at self-induced convection against the higher pressure at the apical region. Meanwhile, it interacts with the ventricular wall and induces the formation of another small vortex ring which developed from a boundary layer. The high pressure energy at the apical region and low vortex strength or kinetic energy of the propagating flow stream restricts the penetration of the vortex ring to the end of the apex in the enlarged chamber. As a result, the vortex ring halts at the mid ventricular region ($t = 0.35$ s). The region beneath the vortex ring remains in a low velocity condition. The same vortex evolution process reprises during late filling, but with a smaller size secondary vortex ring because of lesser inflow volume during the late filling wave.

Conversely, the parabolic flow stream containing high kinetic energy propels the flow stream towards the apex. The parabolic flow stream travels under great inertial influence and is therefore able to approach the middle region of the LV during the acceleration phase ($t = 0.15$ s). No vortex ring is developed in the early filling phase as the flow stream is able to overcome the high pressure at the apical region without being redirected towards the base. The incoming fluid propagates against the resistance of the resting fluid and develops shear layer. During deceleration of the transmitral velocity ($t = 0.25$ s), the parabolic flow stream is decelerated progressively by the accumulated pressure energy deposited in the resting fluid as well as local deceleration at the down-stroke of the E wave. However, at this moment, the parabolic flow stream, which has

already reached the lower part of the ventricle, experiences a convective acceleration at the same time due to the decreasing diameter of the ventricle at the apex ($t = 0.25$ s). Once the energetic parabolic flow comes in contact with the myocardial wall at the end of the apex, the flow stream is reflected and redirected towards the basal region. As a consequence of the interaction between the flow stream and the myocardial wall, a boundary layer is formed near the wall which contains vorticity rotating in opposite direction with that of the parabolic flow. This boundary layer develops into small vortices which interact among each other and with the ventricular wall to produce strong vorticity as observed during diastasis ($t = 0.35$ s). The same process is repeated during the late filling phase.

The instantaneous vortex strength in both the uniform and parabolic flow studies is shown in Figure 4.3, where the maximum vortex strength in the LV with a parabolic inlet velocity profile ($0.38 \text{ m}^2/\text{s}$) is almost 2 times greater than that using a uniform inlet velocity profile ($0.22 \text{ m}^2/\text{s}$). The maximum vortex strength occurs during early filling in the first scenario (using a parabolic inlet velocity profile) but during late filling in the second scenario (using a uniform inlet velocity profile).

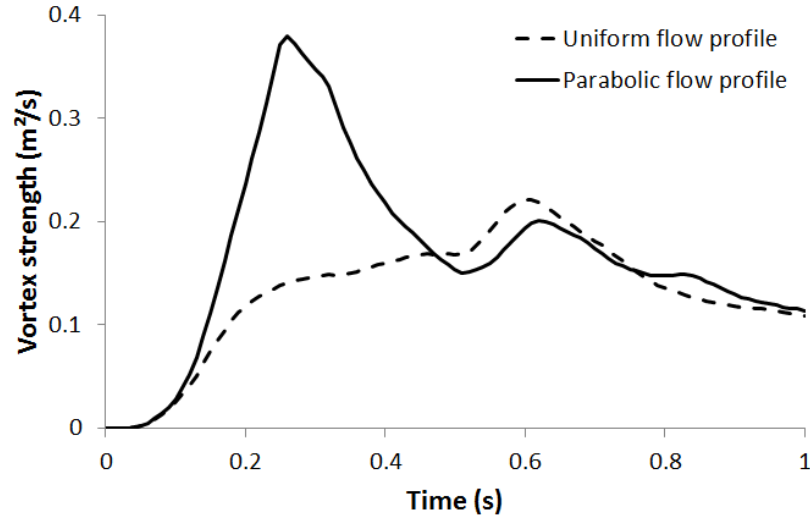


Figure 4.3: Vortex strength in a DCM ventricle with different spatial velocity profile.

4.2. Geometry-prescribed vs. FSI method

In order to compare different implementation of CFD method, three LV models with different ESV, i.e. normal (50 mL), moderate dilated (150 mL) and severely dilated (300 mL) were simulated using both geometry-prescribed and FSI methods. The result similarity and disparity obtained from the two different methods were evaluated.

Figure 4.4 shows a comparison of the vortex distribution in the ventricle under the three different cardiac conditions through implementation of geometry-prescribed and FSI method. In both simulations, the propagating vortex ring in dilated ventricles has less interaction with the ventricular wall, thereby producing a thinner boundary layer. The most notable difference between the two implementations lies in the vortex attachment to the edge of the mitral orifice. In the FSI implementation results, the vortex ring was attached to the edge of the mitral orifice for a longer period. In addition, a

thinner boundary layer was observed, and less interaction occurred between the vortex and the wall. Dissimilar with the geometry-prescribed method, wall expansion of the FSI model depends on the fluid force exerted on it. Furthermore, due to the fixed constraint at the basal wall, there is a slight difference between the two methods in regards to the geometry, especially at the basal region of the ventricle, which leads to the difference in the result.

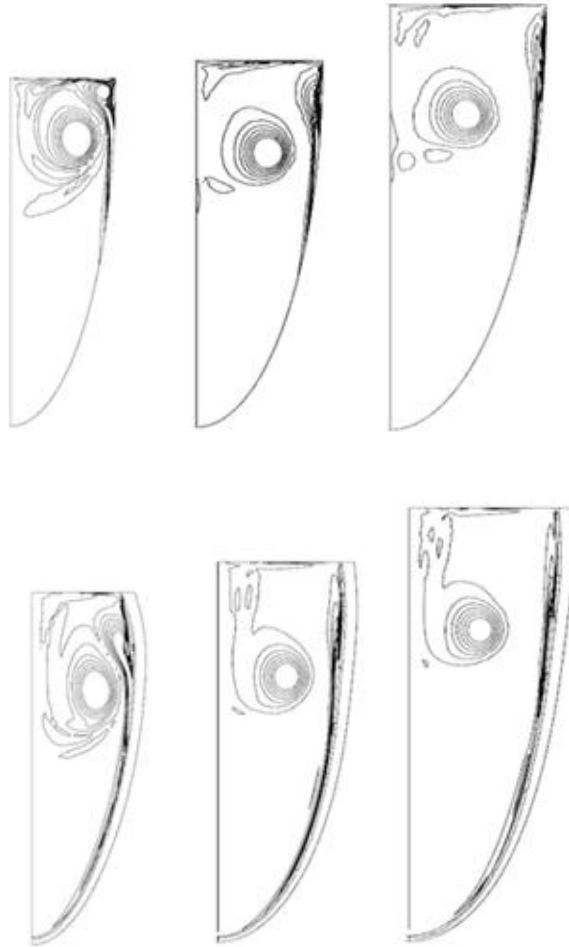


Figure 4.4: Instantaneous vorticity in the normal, moderately dilated and severely dilated LV at $t = 0.36$ s in the geometry-prescribed (top) and FSI implementation (bottom), vorticity levels (1/s) from 5 to 100, step 10.

As expected in both methods, vortex strength in the more dilated ventricles is lower as compared to the normal condition. Comparing the three different cardiac conditions, the normal ventricle has the greatest vortex strength (maximum strength of $0.04378 \text{ m}^2/\text{s}$) as compared to the moderately (maximum strength of $0.03782 \text{ m}^2/\text{s}$) and severely dilated ventricle (maximum strength of $0.03513 \text{ m}^2/\text{s}$), as shown in Figure 4.5.

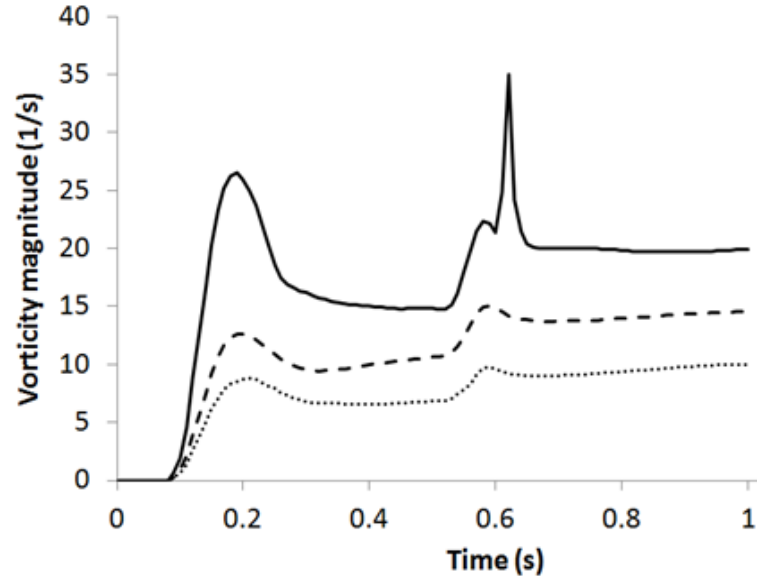


Figure 4.5: Vorticity magnitude in normal (solid line), moderately dilated (dashed line) and severely dilated LV (dotted line).

Compared to the geometry-prescribed method, FSI approach provides additional parameters such as myocardial displacement and wall stress, which serve as useful prognostic determinants of heart disease. The wall movement depends on the wall properties and the fluid force exerted on it. Figure 4.6 shows that the wall displacement and velocity were significantly reduced by ventricular dilatation at the same inflow volume and wall properties.

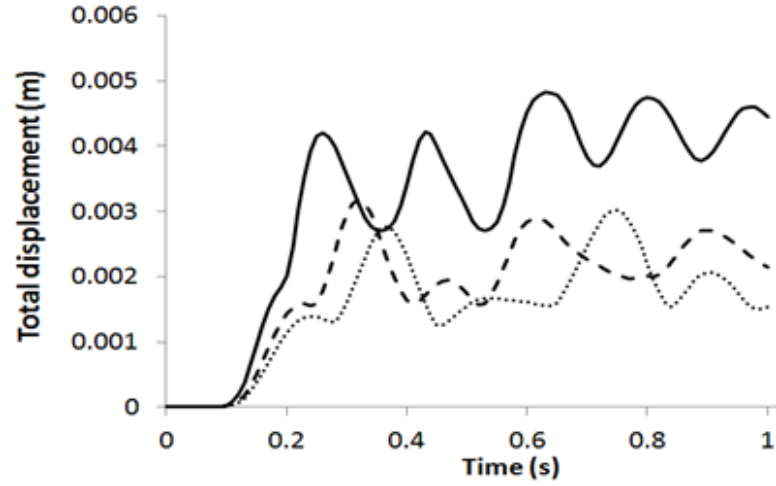


Figure 4.6: Total displacement (right) of normal (solid line), moderately dilated (dashed line) and severely dilated LV (dotted line) obtained from FSI implementation.

4.3. Normal, IDCM, and ICM conditions

4.3.1. Intraventricular flow distribution

Figure 4.7 shows the vorticity contour plot in the normal LV, IDCM (impaired relaxation), and ICM (impaired relaxation) conditions during the peak E-wave, end of E-wave, and end of filling phase. In all cases, as blood flows across the mitral orifice to the larger ventricular chamber, it decelerates and thus pressure increases. The higher pressure downstream opposes the incoming blood flow and redirects it, forming a recirculation structure known as vortex ring. Meanwhile, the vortex induces the formation of boundary layers at the ventricular wall due to viscous adherence condition at the wall. The vortex creates local velocity gradient along the wall and this perturbation gives rise to a vortex-induced separation of the boundary layer, which rotates in the opposite direction. At end of E-wave, the vortex has travelled mid way into the LV axis in all cases. A secondary vortex ring induced by the atrial contraction can be observed in all cases at end of filling.

Notable differences can be observed between the normal and the DCM cases in terms of the vorticity distribution (Figure 4.7). However, the vorticity distribution in the IDCM condition is similar to that in the ICM condition. It can be seen that the vortices in the DCM cases have a more spherical shape, as compared to that in the normal condition, where they are more elongated in shape. Furthermore, the relative area occupied by the vortices compared to that of the total LV area is much higher in the normal condition. Although the propagation velocity of the vortices is similar among the three conditions, the vortex did not reach the apical region during end filling in both DCM cases, in contrary to that in the normal case, due to a difference in their LV size.

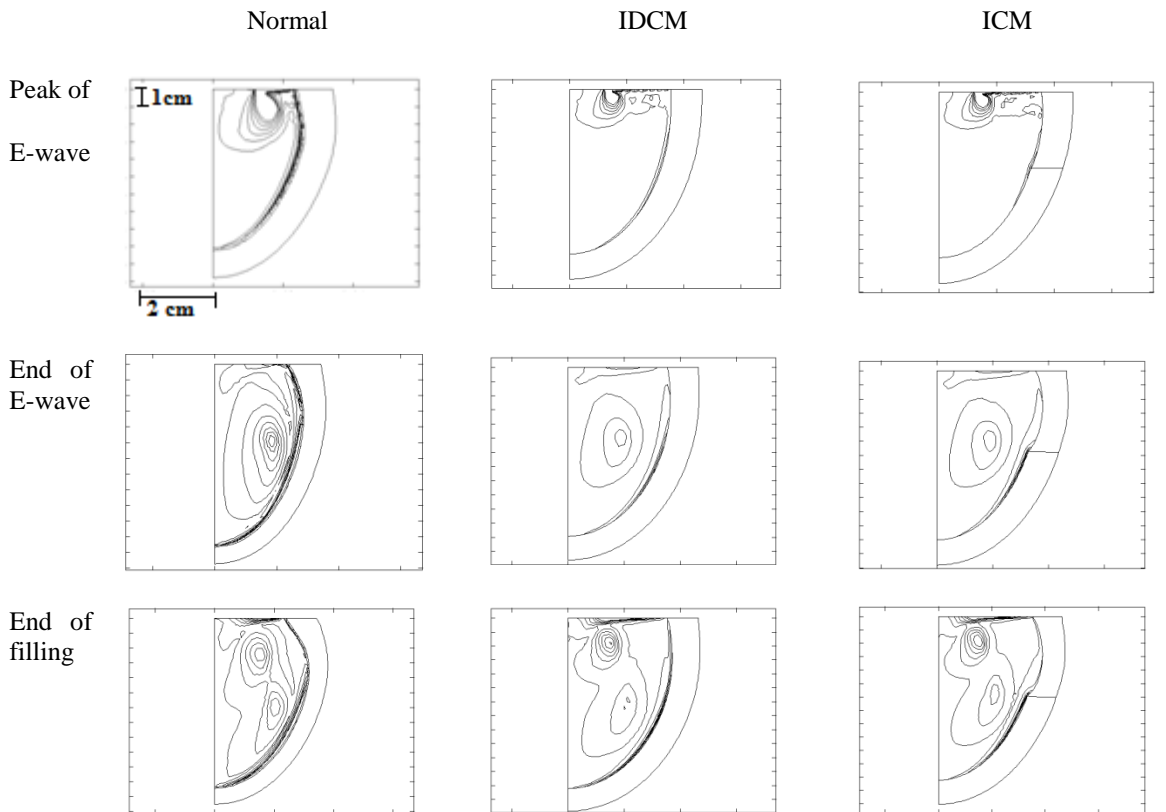


Figure 4.7: Instantaneous vorticity (contour plot) in normal LV, IDCM (impaired relaxation) and ICM (impaired relaxation).

Among the different filling patterns, the restrictive filling pattern yields the highest ϖ , followed by pseudonormal and impaired relaxation filling patterns. Both DCM conditions have a higher Γ_A as compared to the normal LV condition. On the other hand, DCM conditions with a restrictive filling pattern has the highest Γ_I , followed by the normal LV condition, DCM conditions with a pseudonormal filling pattern, and lastly DCM conditions with an impaired relaxation pattern. V_p is higher in the normal LV compared to the DCM conditions. Meanwhile, among the various filling patterns, DCM condition with a restrictive filling pattern has the greatest V_p , followed by pseudonormal and impaired relaxation.

4.3.2. Intraventricular pressure, wall stress, and strain distribution

Figure 4.8 illustrates the temporal waveforms of the IVPD for normal, IDCM, and ICM conditions with different filling patterns. Generally, normal LV shows the greatest fluctuations throughout the filling phase. It can be observed that early peak IVPD occurs during the acceleration phase of E-wave (peak acceleration) in all cases. DCM conditions with a restrictive filling pattern have the highest early peak IVPD, followed by DCM conditions with a pseudonormal filling pattern, normal LV, and lastly DCM conditions with impaired relaxation. On the contrary, among the different conditions, DCM conditions with a restrictive filling pattern have the lowest late peak IVPD.

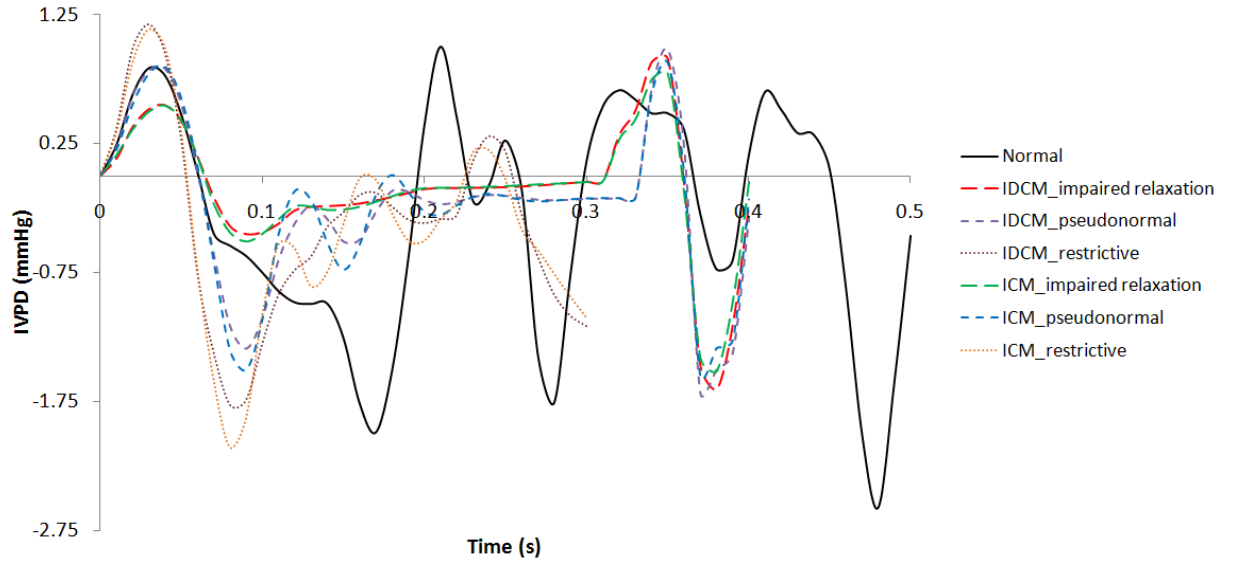


Figure 4.8: Temporal waveforms of the IVPD for normal, IDCM, and ICM with impaired relaxation, pseudonormal and restrictive filling patterns.

Figure 4.9 shows the von Mises stress (vMs) and strain distribution in the normal LV, IDCM (impaired relaxation), and ICM (impaired relaxation) cases during end of the filling phase. The findings indicate a decreasing transmural stress distribution from the endocardial to the epicardial wall in all cases during the filling phase. On the other hand, average transmural stress at the mid-height level is higher as compared to the apical region. ICM condition demonstrates high wall stress at the border zone between the ischemic and the non-ischemic region.

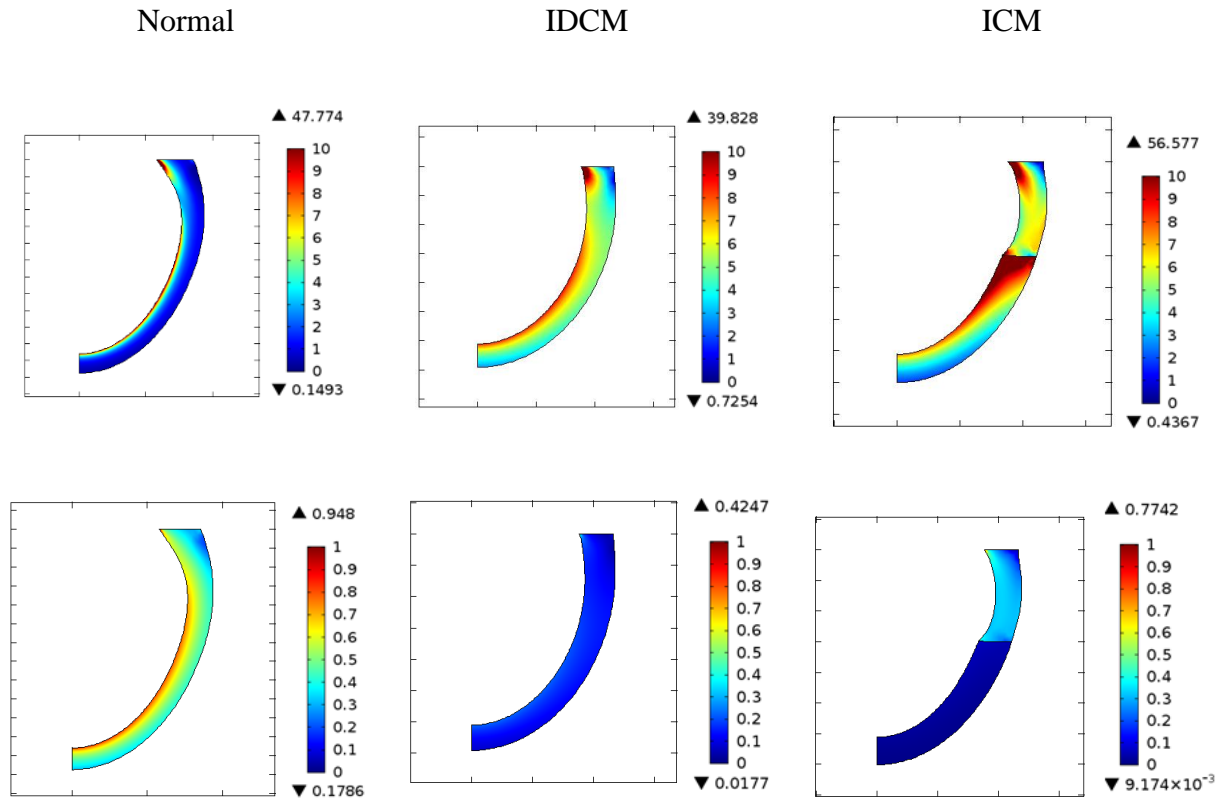


Figure 4.9: vMs (top) and strain (bottom) distribution for (a) normal, (b) IDCM (impaired relaxation) and (c) ICM (impaired relaxation) during end of the filling phase.

Table 4.1 shows the quantitative result of intraventricular fluid dynamics and wall mechanics. Compared to the normal LV case, the average wall stress for the DCM conditions is much higher (Table 4.1). On the contrary, normal LV exhibits the greatest strain and strain rate in all directions, i.e. longitudinal, circumferential, and radial directions (Figure 4.9 & Table 4.1). The ischemic region in the ICM condition has much lower strain level as compared to other regions along the myocardial wall (Figure 4.9).

Table 4.1: Quantitative comparison of various intraventricular fluid dynamics and myocardial wall mechanics measurements for normal, IDCM and ICM with impaired relaxation, pseudonormal and restrictive filling patterns.

	Normal	IDCM			ICM		
		Impaired	Pseudo	Restrictive	Impaired	Pseudo	Restrictive
$\overline{\omega}$ (1/s)	8.90	3.47	5.52	7.29	3.66	5.74	7.49
Γ_A (m ²)	2.21	2.26	2.72	2.71	2.31	2.64	2.67
Γ_I (m ² /s)	0.011	0.006	0.010	0.013	0.006	0.010	0.013
V_p (m/s)	0.445	0.150	0.286	0.357	0.098	0.259	0.357
IVPD _E (mmHg)	0.833	0.548	0.828	1.17	0.543	0.841	1.14
IVPD _L (mmHg)	0.644	0.908	0.979	0.306	0.788	0.871	0.196
vMS (kPa)	0.844	3.06	3.60	3.682	2.849	3.57	3.667
SR _L	0.655	0.21	0.208	0.281	0.230	0.231	0.308
SR _C	0.509	0.154	0.152	0.207	0.0756	0.0754	0.1002
SR _R	-0.574	-0.246	-0.244	-0.329	-0.165	-0.166	-0.221

$\overline{\omega}$ = average vorticity, Γ_A = vortex area, Γ_I = vortex intensity, Γ_{ave} = average vorticity, V_p = flow propagation velocity, IVPD_E = early peak intraventricular pressure difference (IVPD), IVPD_L = late peak IVPD, average vMS = average von Mises stress, SR_L = average longitudinal strain rate, SR_C = average circumferential strain rate, SR_R = average radial strain rate.

4.3.3. PV relationship

Figure 4.10 shows the LV PV curve obtained throughout the filling phase in all cases. It is shown that the PV curve is shifted to the right in the DCM cases, with an increase in slope. Although both DCM cases have the same initial and end PV points, they traverse a slightly different path, with the ICM appearing to be more compliant within the range used in the current study.

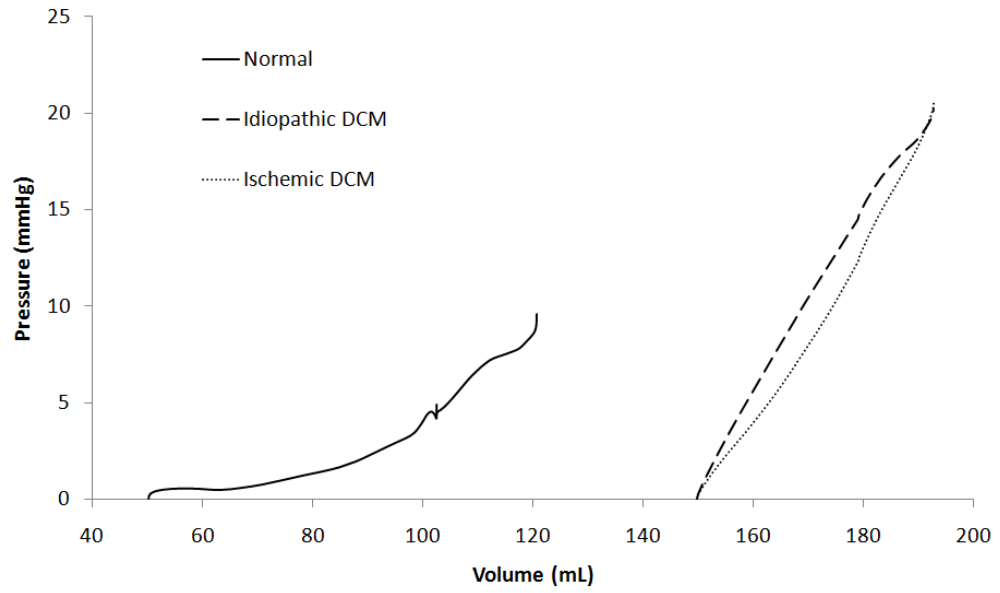


Figure 4.10: PV relationship for normal, IDCM and ICM conditions throughout the filling phase.

4.4. Sensitivity analysis

Figure 4.11 and Figure 4.12 illustrate the percentage change in vortex intensity, Γ_I , V_p , early peak IVPD, EDP, as well as vMS , SR_L , SR_C , and SR_R of the myocardial wall with a two times increase in the peak E-wave velocity (maintaining E/A ratio and DT), ESV, wall stiffness and SI from their respective baseline values. In Figure 4.11, the baseline values of E peak = 0.7 m/s, ESV = 50 mL, SI = 0.52 and wall stiffness are the same as the normal condition as demonstrated in Section 4.3.

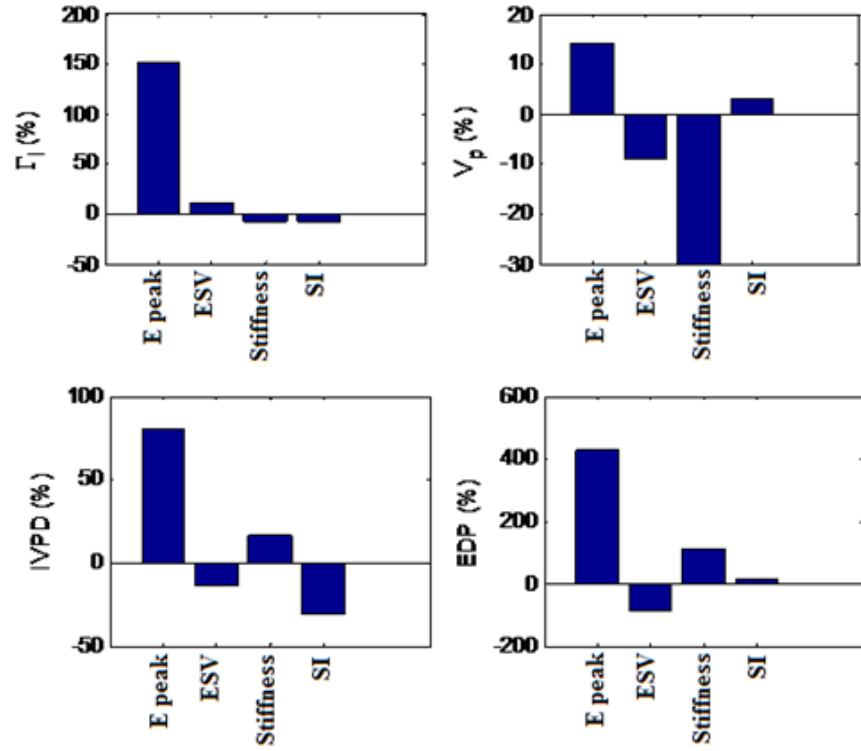


Figure 4.11: Effects of DCM parameters on fluid dynamic measurements.

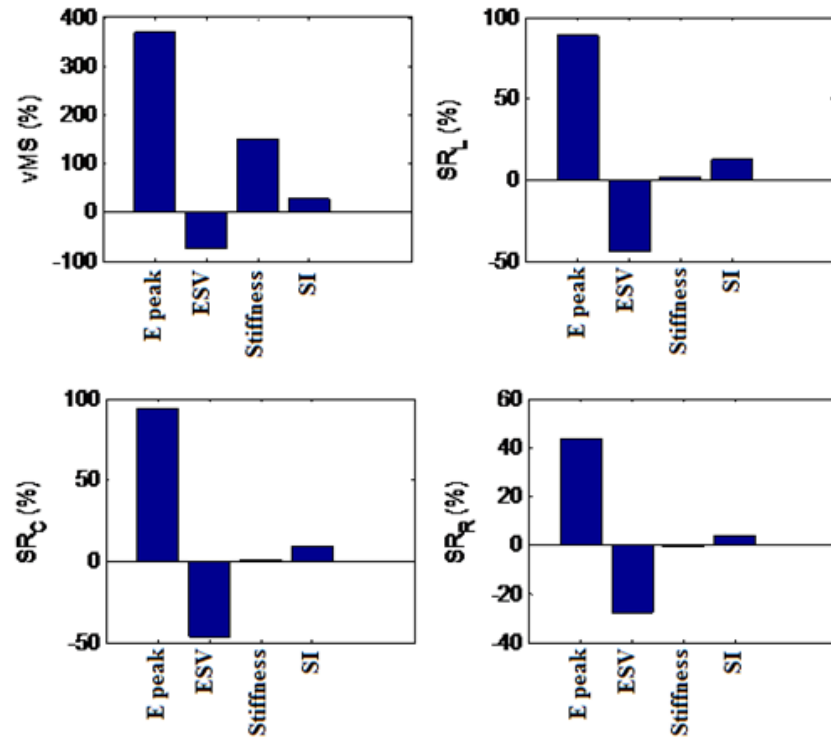


Figure 4.12: Effect of DCM parameters on wall mechanics measurement.

Peak E-wave velocity contributes the most to Γ_I , with a percentage increase of 151.6%, which is far higher than the other factors. Wall stiffness causes the most significant effect on V_p (-30%), followed by peak E-wave velocity (14.4%), ESV (-9%) and SI (3%). On the other hand, IVPD increases with an increase in the peak E-wave velocity (80.3%) and wall stiffness (17%), but decreases with increasing SI (-30.9) and ESV (-14.3%). EDP and vMS follow similar trends, with peak E-wave velocity contributing the most (431.5% and 371.6%), followed by wall stiffness (113.1% and 149.8%), ESV (-83% and -73.4%), and SI (13.3% and 28.9%). With regards to peak strain rates, an increase in the peak E-wave velocity causes a substantial increase in the strain rates (SR_L : 140.7%, SR_C : 131.1%, SR_R : 80.0%). To the contrary, increasing ESV significantly decreases strain rates (SR_L : -44.5%, SR_C : -46.4%, SR_R : -28.0%). SI and wall stiffness, on the other hand, have negligible effects on strain rates.

Chapter 5. DISCUSSION

5.0. Introduction

The discussion part is divided into four sections. Firstly, the vortex evolution of uniform and parabolic transmitral velocity profile is discussed. It is followed by the comparison between two CFD methods, i.e. geometry-prescribed and FSI implementation. The comparison among normal and DCM LVs were discussed in the subsequent section. The last section of discussion concentrates on sensitivity analysis of individual factors which have been observed in DCM LV.

5.1. Comparison between uniform and parabolic velocity profile

While blood flows across the narrow mitral orifice to the broader ventricular chamber, blood decelerates and pressure increases simultaneously in the direction of flow according to the conservation of mass and Bernoulli's principle. The higher pressure at the downstream opposes the incoming flow stream, leading to a fan-like flow towards the ventricular wall. As a result, the flow stream tends to roll up and redirect towards the mitral valve (Pasipoularides et al., 2003).

The vortex formation pattern in the LV with a uniform inlet velocity profile agrees with that reported in the literature, where the vortex ring is attached to the mitral edge until the diastasis phase. In addition, instead of moving vertically downward towards the apex as observed in the LV with a parabolic inlet velocity profile, the vortex ring is enlarged in the dilated LV and extended axially towards the side wall of the

ventricle (Baccani et al., 2002b; Garcia et al., 1998). As a result, the vortex ring is not able to reach the end of the apex to wash out the apical stagnant flow, leading to an increase in the risk of thrombus formation at the apex. Conversely, simulation study using a parabolic inlet velocity profile yields a deviated vortex pattern compared to that observed clinically, where the incoming flow travels straight down to the end of the apex with higher vortex strength.

The difference in the vortex formation pattern and vortex strength using the two different spatial inlet velocity profiles can be explained through the use of the kinetic energy factor, α (Cengel & Cimbala, 2006), i.e. the ratio of the actual kinetic energy. With identical average inflow rate, parabolic flow stream travels with a maximum velocity (2 m/s, at the middle of the LV) of about twice that of the uniform flow stream (1 m/s), although both velocity profiles have comparable average velocity. In a laminar flow condition, the kinetic energy factor, which is associated with the spatial velocity profile, is extremely important because it affects the kinetic energy and the velocity of the flow stream. The parabolic inlet velocity profile produces a kinetic energy factor which is two-fold higher compared to that using the uniform inlet velocity profile.

The vortex evolution pattern acts as an important cardiac health assessment because it reveals the risk of apical thrombosis in the dilated (Maze et al., 1989). Several studies have been carried out to investigate the effect of the intra-ventricular vortex flow pattern on the normal (Baccani et al., 2002a; Vierendeels et al., 2000) and the diseased ventricles (Baccani et al., 2002b; Domenichini & Pedrizzetti, 2011; Pasipoularides et al., 2003), using echocardiography (D'cruz & Sharaf, 1991) and

magnetic resonance imaging (Schenkel et al., 2008) as validation tools. In a normal ventricle, the incoming flow is redirected towards the base by the higher pressure at the downstream, thus forming a vortex ring attaching to the mitral edge. During deceleration of the E-wave, this vortex ring is detached from the mitral edge and moves freely towards the apex region with a high vortex strength. As a result, the vortex ring is able to reach the end of the LV apex during the filling phase (Baccani et al., 2002b; Vierendeels et al., 2000). On the contrary, the vortex movement is restricted in a DCM ventricle due to a longer period of vortex attachment at the mitral edge. The DCM ventricle produces a lower vortex strength which is insufficient to propagate the vortical flow towards the bottom of the LV (Chan et al., 2012).

In short, by comparing to parabolic velocity profile, the uniform velocity profile demonstrated vortex evolution process which strongly agreed with published studies as mentioned above. Hence the uniform velocity profile was confirmed and selected as boundary condition in the simulation of DCM conditions.

5.2. Comparison between geometry-prescribed and FSI method

By using prescribed geometry approach, the vortex formation and movement patterns in the simulations generally agreed with that shown in the published literature (Baccani et al., 2002b; Cheng et al., 2005). Generally, the results obtained from the FSI implementation show a good agreement with the geometry-prescribed approach. The vorticity result generally agrees with data from published simulations (Loerakker et al., 2008) and experimental results (Hong et al., 2008), which provided quantitative vortex

measurements. The vorticity magnitude shown in Figure 4.5 was contributed by both the primary (peak of E wave) and secondary vortices (peak of A wave), as well as the growing boundary layer. A high vorticity magnitude helps the propagation of the vortex ring towards the apex. Due to the weaker vortex strength in a more dilated ventricle, the vortex ring is propelled towards the apex by weaker convective acceleration and thus has less energy. As a result, vortex washout is reduced, leading to the stagnation of the apical flow region. In an experimental study, Maze et al. (1989) reported that thrombus formation was commonly found in dilated ventricles associated with cardiomyopathy.

Compared to the geometry-prescribed method, FSI approach provides additional parameters such as myocardial displacement and wall stress, which serve as useful prognostic determinants of heart disease. An increase in wall stress increases the risk for arrhythmia and energy metabolism, which forces the dilated ventricle to work even harder. The wall movement depends on the wall properties and the fluid force exerted on it. The wall displacement and velocity were significantly reduced by ventricular dilatation at the same inflow volume and wall properties. The decreasing wall velocity indicated loss of elastic recoil energy which contribute to impaired diastolic suction and contractile function for blood ejection during systole (Sonnenblick, 1980; Yotti et al., 2005). By comparing CFD implementation method, FSI method is chosen for this DCM study because of equally important roles of both blood flow and myocardial wall mechanics in the DCM defects.

5.3. Simulation of normal, IDCM, and ICM conditions

The abnormal flow pattern in diseased LV is often associated with thrombus formation where flow stasis region promotes blood clot formation and contributes to low V_p . Thrombus formation, particularly at the apical region of the LV, has frequently been reported in patients with DCM (Falk et al., 1992). It is believed that this is associated with low vortex intensity (Loerakker et al., 2008) and V_p (Baccani et al., 2002b). During the filling phase, the formation of vortex ring aids in preserving the kinetic energy of the incoming flow through fast rotating motion (Pasipoularides et al., 2003) and induces blood exchange to prevent flow stagnation (Eriksson et al., 2012). As the vortex ring rotates around its center of mass while translating from the base to the apex, the total kinetic energy of the incoming blood flow is converted into rotational and translational energy (Hanc & Taylor, 2004). The translational energy allows penetration of the vortex ring to the stagnant flow region at the apex, while blood mixing is enhanced by the rotational energy.

Despite the importance of vortex on intraventricular flow dynamics, not many studies have quantitatively analyzed vortex-related parameters in a LV computational model. While Loerakker et al. (2008) observed a decreased vortex area and vortex intensity in a computational model of LV with DCM, opposite results were obtained by Baccani et al. (2002b) which used the same filling velocity for both normal and DCM conditions. The above contradictory result can be explained by the current study, which shows that filling velocity is the prime determinant of vortex intensity due to its close relationship with kinetic energy. On the other hand, an increase in the LV size as in (Baccani et al., 2002b) causes an increase in the vortex area and a minor increase in the

vortex intensity, due to a larger space for growth of the vortex ring. Although it was observed lower vortex intensity in the normal LV in the simulation results when compared to DCM with a restrictive filling pattern, stronger vorticity field and thus higher average vorticity is obtained in the normal LV, due to a larger vortex-LV relative area. Furthermore, as the vortex approaches the compliant LV wall, it induces a substantial perturbation in the pressure field near the wall which causes a significant deformation of the wall (Alben, 2011), thereby preventing flow stagnation.

With the availability of myocardial deformation imaging technology, diastolic strain rate, which characterizes the speed of myocardial deformation during the diastolic phase, has become increasingly popular for the assessment of diastolic function (active relaxation) (Zeng et al., 2009) as well as the identification of myocardial infarct size and location (Zhang et al., 2005). The simulation results agree with the published literature (Duan et al., 2012; Park et al., 2006), which reported reduced longitudinal and circumferential diastolic strain rates in patients with DCM. A decrease in the diastolic strain rate leads to impaired filling efficiency and potentially reduces the contraction force during ejection. Since myocardial deformation (LV expansion) is directly related to the filling velocity, peak E-wave velocity contributes the most to strain rates in all directions as compared to other factors. This is in agreement with clinical findings, which reported that strain rate measurements are significantly dependent on preload (Voigt et al., 2002). A major advantage of the diastolic strain rate over filling velocity in the assessment of diastolic function is its ability to describe regional myocardial function. The simulation results showed that strain rate along the infarcted region (apex) of the myocardial wall is substantially lower than other regions of the wall. This is in

agreement with clinical findings (Pislaru et al., 2004), which reported significant correlation between early strain rate and regional stiffness, and proposed that segmental diastolic strain rate can indicate the presence and extent of regional ischemia (Hung et al., 2008).

5.4. Sensitivity analysis

While V_p has been proven to be a relatively preload-independent index of diastolic function through various clinical studies (Garcia et al., 1998), its value is still debated in patients with hypertrophic (Buakhamsri et al., 2009) and restrictive DCM (Garcia et al., 1996). The current study reveals that V_p is substantially (30%) decreased by a twofold increase in wall stiffness, thus it forms a useful index for passive chamber compliance. This agrees with De Boeck et al. (2005), who suggested that an increase in wall stiffness lead to an increase in pressure wave propagation velocity (principle of acoustic conduction) which in turn slows down the propagation of the velocity wave. On the other hand, a decrease in LV size (ESV) causes an increase in V_p , as it provides a narrow path which directs the propagation of flow velocity downwards. The results may explain the high V_p values obtained in patients with hypertrophic LV. With regards to the effect of preload on V_p , the results showed a positive correlation between peak E-wave velocity and V_p . Upon closer investigation, it was found that V_p increases exponentially with peak E-wave velocity, i.e. an increase in peak E-wave velocity causes a minor increase in V_p at low values, but significantly increases V_p at high velocity. Consequently, preload-independency may be weakened in patients with high E-wave velocity.

Generation of sufficient IVPD improves the efficiency of early diastolic LV filling (Yotti et al., 2005). Extensive studies have reported that the prime determinant of early peak IVPD is elastic recoil and myocardial relaxation rate (Firstenberg et al., 2001). In the present study, it was found that early peak IVPD coincides with peak acceleration of the E-wave in all cases, with its magnitude correlates positively with the rate of change of the filling velocity, which is in turn dependent on the myocardial relaxation rate in a real clinical setting. On the other hand, an increase in ESV decreases peak early IVPD. The results is in agreement with Yotti et al. (2005), who proposed that early peak IVPD is influenced mainly by inertial acceleration (rate of change of the filling velocity) and convective deceleration which depends on the ventriculo:annular disproportion.

With regards to EDP and vMS, the simulation results showed that both parameters are substantially raised in the DCM conditions, mostly due to an increase in wall stiffness. An increase in ESV and SI, which is associated with adverse ventricular remodelling process, causes opposite effects on EDP and vMS, with the former decreases EDP and vMS while the latter causes an increase in both EDP and vMS. High stress is found near the border zone between the ischemic and the non-ischemic region, as observed by Jackson et al. (2003), and it is believed that this may further worsen the myocardial function around the region (Jackson et al., 2003).

Chapter 6. CONCLUSION

6.0. Conclusion

When blood enters the LV from the mitral valve, the change of the geometrical dimensions and the short mitral valve length disables the laminar blood flow to be fully developed into a parabolic profile. As a result, incoming blood enters the LV with a uniform velocity profile during the filling phase. It is shown from the current study that the transmitral velocity profile significantly affects the intra-ventricular vortex flow pattern. The resulting vortex evolution pattern using the uniform inlet velocity profile agreed with that reported in the literature, which revealed an increase in thrombus risk in a ventricle with DCM. On the other contrary, the application of a parabolic velocity profile at the inlet yields a deviated vortical flow pattern and overestimates the propagation velocity of the vortex ring towards the apex of the ventricle. The present work confirmed that the transmitral spatial velocity profile appears in uniform velocity profile rather than parabolic velocity profile.

The effects of geometrical modification in a ventricle on the intraventricular flow distributions were simulated using two different models, i.e. the geometry-prescribed and FSI method. Although similar simulation results were obtained from the two methods, FSI approach provides additional information such as wall stress and strain, which are important predictors of ventricular function. Moreover, cardiac diseases can be more easily and realistically modelled using the FSI method compared to the geometry-prescribed method, which may involve more complicated equations and

assumptions that often results in convergence problem. As such, FSI implementation was selected for further simulation study of DCM disease.

A 2D axisymmetrical FSI model of a LV under normal and DCM conditions (IDCM and ICM) have been presented in this work, and the effect of DCM on intraventricular fluid dynamics and myocardial wall mechanics were investigated. Intraventricular flow dynamics and myocardial wall deformation are significantly impaired in the DCM conditions, with low vortex intensity, V_p , IVPD and strain rates, but high EDP and wall stress.

The sensitivity analysis results show that V_p substantially decreases with an increase in wall stiffness, and is relatively independent of preload at low peak E-wave velocity. Early IVPD is influenced mainly by the rate of change of early filling velocity and ESV which changes ventriculo:annular disproportion. Regional strain rate, on the other hand, is significantly correlated with regional stiffness, and therefore forms a useful indicator for myocardial regional ischemia. The present work forms an important framework for the investigation of mechanisms leading to observable changes in patients with DCM which is important for the clinical management of these patients.

6.1. Limitation and recommendation for future works

There are several limitations in the current study which requires further improvements. During LV filling simulation, the implementation of fixed constraint at the basal location of the FSI boundary causes exceptionally high stress around that point

as the wall movement was restricted at the constrained boundary. This may result in an inaccurate stress analysis at the basal region, especially near the constrained site thus instant improvement is needed to sort out this limitation.

The use of axisymmetrical model in this study may affect the pathway of blood flow and vortex propagation as well. It is suggested that an asymmetrical LV geometry or patient specific model should be incorporated in future studies. Aside from interaction between blood and heart muscle, an integration of electrophysiology model present a more complete computational heart model. Furthermore, the integration with other heart chambers, such as left atrium and right ventricle, provides the full pathway of cardiac blood flow and produce a more precise interaction analysis.

In this study, the mitral valve was modelled as an opening orifice and non-moving structure, which should be further developed into a moving structure. Additionally, incorporation of myocardial fiber in the LV wall is suggested to be developed, in order to produce a more realistic regional strain and stress distributions along the LV wall.

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APPENDIX

A simplified relation from an elastic membrane model is used to infer the relative dynamics of LV wall by assuming that LV is a half truncated prolate ellipsoidal geometry and has linear elastic wall behaviour.

According to Laplace's law, the force imposed on the LV chamber due to blood pressure is balanced by a reaction force caused by the LV wall stress. The meridional stress, σ_ϕ and circumferential stress, σ_θ , are the LV wall stresses involved.

Meridional wall stress is balanced by the pressure, p , across circular cross section area of LV short axis:

$$\sigma_\phi(2\pi R) = p(\pi R^2)$$

$$\sigma_\phi = \frac{pR}{2} \tag{i}$$

Circumferential wall stress is balanced by the pressure across ellipsoidal area of LV long axis:

$$\sigma_\theta \left(\frac{4\pi H^3}{8H^2 - 4R^2} \right) = p \left(\frac{\pi RH}{2} \right) \tag{ii}$$

where R represents the radius and H represents height of LV geometry.

By applying linear elasticity relation ($\sigma = E\varepsilon$), where E is Young's modulus, the meridional and circumferential wall stress can also be represented as:

$$\sigma_\phi = E \frac{dR}{R} \tag{iii}$$

$$\sigma_{\theta} = E \frac{dH}{H} \quad (\text{iv})$$

Mathematically, substituting Equation (iv) into (iii), Equation (v) is obtained as:

$$\frac{dH}{H} = \frac{4H^2}{8H^2 - D^2} \left(\frac{dR}{R} \right) \quad (\text{v})$$

By differentiation, the relationship of rate changes of radius ($\frac{dR}{dt}$) and height ($\frac{dH}{dt}$) are:

$$\frac{dH}{dt} = \frac{H}{R} \left(\frac{4H^2}{8H^2 - 4R^2} \right) \left(\frac{dR}{dt} \right) \quad (\text{vi})$$

However, the independent equations of the rate change of radius and height are required in the model application. The independent equations can be established through LV volume equation by assuming LV is a half truncated prolate ellipsoidal geometry:

$$V = \frac{2\pi}{3} R^2 H \quad (\text{vii})$$

According to mass conservation law, blood inflow rate, $Q(t)$, equals to the rate change of LV volume:

$$Q(t) = \frac{dV}{dt} = \frac{2\pi}{3} \left(R^2 \frac{dH}{dt} + 2RH \frac{dR}{dt} \right) \quad (\text{viii})$$

After the mathematical substitution involving Equation (vi) into (viii), the independent equations of the rate changes of LV radius and height are therefore obtained as:

$$\frac{dR}{dt} = \frac{3Q(t)}{\pi} \left(\frac{2H^2 - R^2}{10H^3 R - 4HR^3} \right) \quad \text{Equation (3.3)}$$

$$\frac{dH}{dt} = \frac{3Q(t)}{\pi} \left(\frac{H^3}{2H^2 R - R^3} \right) \left(\frac{2H^2 - R^2}{10H^3 R - 4HR^3} \right) \quad \text{Equation (3.4)}$$

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